SECTION 1 (Maximum Marks: 12)

- This section contains FOUR (04) questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme: *Full Marks* : +3 If ONLY the correct option is chosen; *Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered); *Negative Marks* : -1 In all other cases.

Q.1 Let \mathbb{R} denote the set of all real numbers. Let $a_i, b_i \in \mathbb{R}$ for $i \in \{1, 2, 3\}$. Define the functions $f: \mathbb{R} \to \mathbb{R}$, $g: \mathbb{R} \to \mathbb{R}$, and $h: \mathbb{R} \to \mathbb{R}$ by

$$f(x) = a_1 + 10x + a_2x^2 + a_3x^3 + x^4,$$

$$g(x) = b_1 + 3x + b_2x^2 + b_3x^3 + x^4,$$

$$h(x) = f(x+1) - g(x+2).$$

If $f(x) \neq g(x)$ for every $x \in \mathbb{R}$, then the coefficient of x^3 in h(x) is

(A)	8
(B)	2
(C)	-4
(D)	-6

Q.2

Three students S_1 , S_2 , and S_3 are given a problem to solve. Consider the following events:

- *U*: At least one of S_1 , S_2 , and S_3 can solve the problem,
- *V*: S_1 can solve the problem, given that neither S_2 nor S_3 can solve the problem,
- W: S_2 can solve the problem and S_3 cannot solve the problem,

T: S_3 can solve the problem.

For any event E, let P(E) denote the probability of E. If

$$P(U) = \frac{1}{2}$$
, $P(V) = \frac{1}{10}$, and $P(W) = \frac{1}{12}$,

then P(T) is equal to

				-		-	
(A)	13	(B)	1	(C)	19	(D)	1
	36		3		60		4

$$f(x) = \begin{cases} 2 - 2x^2 - x^2 \sin \frac{1}{x} & \text{if } x \neq 0, \\ 2 & \text{if } x = 0. \end{cases}$$

Then which one of the following statements is TRUE?

(A)	The function f is NOT differentiable at $x = 0$
(B)	There is a positive real number δ , such that f is a decreasing function on the interval $(0, \delta)$
(C)	For any positive real number δ , the function f is NOT an increasing function on the interval $(-\delta, 0)$
(D)	x = 0 is a point of local minima of f

Q.4 Consider the matrix

$$P = \begin{pmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{pmatrix}.$$
Let the transpose of a matrix X be denoted by X^T . Then the number of 3×3 invertible matrices Q with integer entries, such that

$$Q^{-1} = Q^T \text{ and } PQ = QP,$$
is
(A) 32 (B) 8 (C) 16 (D) 24

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

	Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;	
	<i>Partial Marks</i> : +3 If all the four options are correct but ONLY three options are chosen;	1
	Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;	1
	Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;	
	Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);	1
	Negative Marks: -2 In all other cases.	
•	For example, in a question, if (A), (B) and (D) are the ONLY three options corresponding to correct	
	answers, then	
	choosing ONLY (A), (B) and (D) will get +4 marks;	
	choosing ONLY (A) and (B) will get +2 marks;	
	choosing ONLY (A) and (D) will get +2 marks;	
	choosing ONLY (B) and (D) will get +2 marks;	
	choosing ONLY (A) will get +1 mark;	
	choosing ONLY (B) will get +1 mark;	
	choosing ONLY (D) will get +1 mark;	
	choosing no option (i.e. the question is unanswered) will get 0 marks; and	
	choosing any other combination of options will get -2 marks.	

Q.5 Let L_1 be the line of intersection of the planes given by the equations

$$2x + 3y + z = 4$$
 and $x + 2y + z = 5$.

Let L_2 be the line passing through the point P(2, -1, 3) and parallel to L_1 . Let M denote the plane given by the equation

$$2x + y - 2z = 6$$

Suppose that the line L_2 meets the plane M at the point Q. Let R be the foot of the perpendicular drawn from P to the plane M.

Then which of the following statements is (are) TRUE?

(A)	The length of the line segment PQ is $9\sqrt{3}$
(B)	The length of the line segment QR is 15
(C)	The area of $\triangle PQR$ is $\frac{3}{2}\sqrt{234}$
(D)	The acute angle between the line segments PQ and PR is $\cos^{-1}\left(\frac{1}{2\sqrt{3}}\right)$

Q.6 Let \mathbb{N} denote the set of all natural numbers, and \mathbb{Z} denote the set of all integers. Consider the functions $f: \mathbb{N} \to \mathbb{Z}$ and $g: \mathbb{Z} \to \mathbb{N}$ defined by

$$f(n) = \begin{cases} (n+1)/2 & \text{if } n \text{ is odd ,} \\ (4-n)/2 & \text{if } n \text{ is even ,} \end{cases}$$

and

$$g(n) = \begin{cases} 3+2n & \text{if } n \ge 0 , \\ \\ -2n & \text{if } n < 0 . \end{cases}$$

Define $(g \circ f)(n) = g(f(n))$ for all $n \in \mathbb{N}$, and $(f \circ g)(n) = f(g(n))$ for all $n \in \mathbb{Z}$.

Then which of the following statements is (are) TRUE?

(A)	$g \circ f$ is NOT one-one and $g \circ f$ is NOT onto
(B)	$f \circ g$ is NOT one-one but $f \circ g$ is onto
(C)	g is one-one and g is onto
(D)	f is NOT one-one but f is onto

Q.7 Let \mathbb{R} denote the set of all real numbers. Let $z_1 = 1 + 2i$ and $z_2 = 3i$ be two complex numbers, where $i = \sqrt{-1}$. Let

$$S = \{ (x, y) \in \mathbb{R} \times \mathbb{R} : |x + iy - z_1| = 2|x + iy - z_2| \}.$$

Then which of the following statements is (are) TRUE?

(A)	S is a circle with centre $\left(-\frac{1}{3}, \frac{10}{3}\right)$
(B)	S is a circle with centre $\left(\frac{1}{3}, \frac{8}{3}\right)$
(C)	S is a circle with radius $\frac{\sqrt{2}}{3}$
(D)	S is a circle with radius $\frac{2\sqrt{2}}{3}$

is

SECTION 3 (Maximum Marks: 24)

- This section contains SIX (06) questions.
- The answer to each question is a **NUMERICAL VALUE.**
- For each question, enter the correct numerical value of the answer using the mouse and the onscreen virtual numeric keypad in the place designated to enter the answer.
- If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme:
 Full Marks : +4 If ONLY the correct numerical value is entered in the designated place;
 Zero Marks : 0 In all other cases.

Q.8 Let the set of all relations *R* on the set $\{a, b, c, d, e, f\}$, such that *R* is reflexive and symmetric, and *R* contains exactly 10 elements, be denoted by S.

Then the number of elements in S is

Q.9 For any two points *M* and *N* in the *XY*-plane, let \overline{MN} denote the vector from *M* to *N*, and $\vec{0}$ denote the zero vector. Let *P*, *Q* and *R* be three distinct points in the *XY*-plane. Let *S* be a point inside the triangle ΔPQR such that

$$\overrightarrow{SP}$$
 + 5 \overrightarrow{SQ} + 6 \overrightarrow{SR} = $\overrightarrow{0}$.

Let E and F be the mid-points of the sides PR and QR, respectively. Then the value of

length of the line segment *EF* length of the line segment *ES*

Q.10 Let S be the set of all seven-digit numbers that can be formed using the digits 0, 1 and 2. For example, 2210222 is in S, but 0210222 is NOT in S.
Then the number of elements x in S such that at least one of the digits 0 and 1 appears exactly twice in x, is equal to ______.

Q.11 Let α and β be the real numbers such that

$$\lim_{x \to 0} \frac{1}{x^3} \left(\frac{\alpha}{2} \int_0^x \frac{1}{1 - t^2} dt + \beta x \cos x \right) = 2.$$

Then the value of $\alpha + \beta$ is _____.

Q.12 Let \mathbb{R} denote the set of all real numbers. Let $f: \mathbb{R} \to \mathbb{R}$ be a function such that f(x) > 0 for all $x \in \mathbb{R}$, and f(x + y) = f(x)f(y) for all $x, y \in \mathbb{R}$.

Let the real numbers $a_1, a_2, ..., a_{50}$ be in an arithmetic progression. If $f(a_{31}) = 64f(a_{25})$, and

$$\sum_{i=1}^{50} f(a_i) = 3(2^{25} + 1),$$

 $\sum_{i=6}^{30} f(a_i)$

then the value of

is

Q.13 For all x > 0, let $y_1(x)$, $y_2(x)$, and $y_3(x)$ be the functions satisfying

.

$$\frac{dy_1}{dx} - (\sin x)^2 y_1 = 0, \quad y_1(1) = 5,$$

$$\frac{dy_2}{dx} - (\cos x)^2 y_2 = 0, \quad y_2(1) = \frac{1}{3},$$

$$\frac{dy_3}{dx} - \left(\frac{2-x^3}{x^3}\right) y_3 = 0, \quad y_3(1) = \frac{3}{5e},$$

respectively. Then

$$\lim_{x \to 0^+} \frac{y_1(x)y_2(x)y_3(x) + 2x}{e^{3x}\sin x}$$

is equal to _

SECTION 4 (Maximum Marks: 12)

- This section contains **THREE (03)** Matching List Sets.
- Each set has **ONE** Multiple Choice Question.
- Each set has TWO lists: List-I and List-II.
- List-I has Four entries (P), (Q), (R) and (S) and List-II has Five entries (1), (2), (3), (4) and (5).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme: *Full Marks* : +4 ONLY if the option corresponding to the correct combination is chosen; *Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered); *Negative Marks* : -1 In all other cases.
- Q.14 Consider the following frequency distribution:

Value	4	5	8	9	6	12	11
Frequency	5	f_1	f_2	2	1	1	3

Suppose that the sum of the frequencies is 19 and the median of this frequency distribution is 6.

For the given frequency distribution, let α denote the mean deviation about the mean, β denote the mean deviation about the median, and σ^2 denote the variance.

Match each entry in List-I to the correct entry in List-II and choose the correct option.

List-I	List-II
(P) $7f_1 + 9f_2$ is equal to	(1) 146
(Q) 19α is equal to	(2) 47
$(\mathbf{P}) 100$ is equal to	(3) 48
(R) 19β is equal to (S) $19\sigma^2$ is equal to	(4) 145
(S) 190 IS equal to	(5) 55

(A)	$(P) \longrightarrow (5)$	$(\mathbf{Q}) \rightarrow (3)$	$(\mathbf{R}) \rightarrow (2)$	$(S) \longrightarrow (4)$
(B)	$(P) \longrightarrow (5)$	$(\mathbf{Q}) \longrightarrow (2)$	$(\mathbf{R}) \longrightarrow (3)$	$(\mathbf{S}) \longrightarrow (1)$
(C)	$(P) \longrightarrow (5)$	$(Q) \rightarrow (3)$	$(\mathbf{R}) \longrightarrow (2)$	$(\mathbf{S}) \longrightarrow (1)$
(D)	$(P) \longrightarrow (3)$	$(Q) \rightarrow (2)$	$(R) \rightarrow (5)$	$(S) \longrightarrow (4)$

Match each entry in List-I to the correct entry in List	t-II and choose the correct option.
List-I	List-II
(P) The minimum value of <i>n</i> for which the function $f(x) = \left[\frac{10x^3 - 45x^2 + 60x + 35}{n}\right]$ is continuous on the interval [1, 2], is	(1) 8
(Q) The minimum value of <i>n</i> for which $g(x) = (2n^2 - 13n - 15)(x^3 + 3x),$ $x \in \mathbb{R}$, is an increasing function on \mathbb{R} , is	(2) 9
(R) The smallest natural number <i>n</i> which is greater than 5, such that $x = 3$ is a point of local minima of $h(x) = (x^2 - 9)^n (x^2 + 2x + 3)$, is	(3) 5
(S) Number of $x_0 \in \mathbb{R}$ such that $l(x) = \sum_{k=0}^{4} \left(\sin x-k + \cos\left x-k + \frac{1}{2}\right \right),$	(4) 6
$x \in \mathbb{R}$, is NOT differentiable at x_0 , is	(5) 10

(A)	$(\mathbf{P}) \longrightarrow (1)$	$(Q) \rightarrow (3)$	$(\mathbf{R}) \longrightarrow (2)$	$(S) \rightarrow (5)$
(B)	$(\mathbf{P}) \longrightarrow (2)$	$(\mathbf{Q}) \longrightarrow (1)$	$(\mathbf{R}) \longrightarrow (4)$	$(S) \to (3)$
(C)	$(\mathbf{P}) \longrightarrow (5)$	$(Q) \rightarrow (1)$	$(\mathbf{R}) \longrightarrow (4)$	$(S) \to (3)$
(D)	$(\mathbf{P}) \longrightarrow (2)$	$(Q) \rightarrow (3)$	$(\mathbf{R}) \longrightarrow (1)$	$(S) \rightarrow (5)$

(D)

Q.16	Let $\vec{w} = \hat{i} + \hat{j} - 2\hat{k}$, and \vec{u} and \vec{v} be two vectors, such that $\vec{u} \times \vec{v} = \vec{w}$ and $\vec{v} \times \vec{w} = \vec{u}$. Let α, β, γ , and t be real numbers such that						
	$\vec{u} = \alpha \hat{\imath} + \beta \hat{\jmath} + \gamma \hat{k}, -t \alpha + \beta + \gamma = 0, \alpha - t \beta + \gamma = 0, \text{ and } \alpha + \beta - t \gamma = 0.$						
	Match each entry in List-I to the correct entry in List-II and choose the correct option.						
	List-I List-II						
	(P) $ \vec{v} ^2$ is equal to (1) 0						
	(Q) If $\alpha = \sqrt{3}$, then γ^2 is equal to (2) 1						
	(3) 2						
	(R) If $\alpha = \sqrt{3}$, then $(\beta + \gamma)^2$ is equal to (4) 3						
	(S) If $\alpha = \sqrt{2}$, then $t + 3$ is equal to (5) 5						
-							
	(A) $(P) \rightarrow (2)$ $(Q) \rightarrow (1)$ $(R) \rightarrow (4)$ $(S) \rightarrow (5)$						
	(B) $(P) \rightarrow (2)$ $(Q) \rightarrow (4)$ $(R) \rightarrow (3)$ $(S) \rightarrow (5)$						
	(C) $(P) \rightarrow (2)$ $(Q) \rightarrow (1)$ $(R) \rightarrow (4)$ $(S) \rightarrow (3)$						

 $(S) \rightarrow (3)$

 $(P) \rightarrow (5) \quad (Q) \rightarrow (4) \quad (R) \rightarrow (1)$

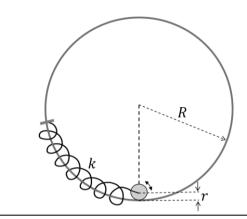
SECTION 1 (Maximum Marks: 12)

- This section contains FOUR (04) questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +3 If **ONLY** the correct option is chosen;

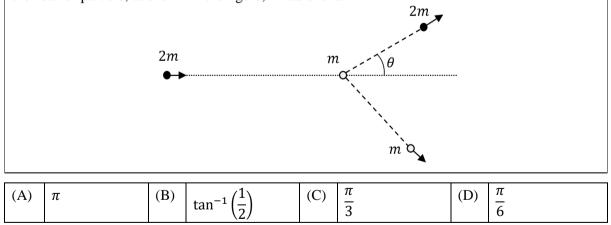
Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered); *Negative Marks* : -1 In all other cases.

Q.1 The center of a disk of radius r and mass m is attached to a spring of spring constant k, inside a ring of radius R > r as shown in the figure. The other end of the spring is attached on the periphery of the ring. Both the ring and the disk are in the same vertical plane. The disk can only roll along the inside periphery of the ring, without slipping. The spring can only be stretched or compressed along the periphery of the ring, following the Hooke's law. In equilibrium, the disk is at the bottom of the ring. Assuming small displacement of the disc, the time period of oscillation of center of mass of the disk is written as $T = \frac{2\pi}{\omega}$. The correct expression for ω is (g is the acceleration due to gravity):

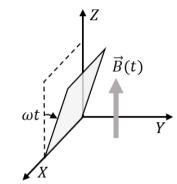


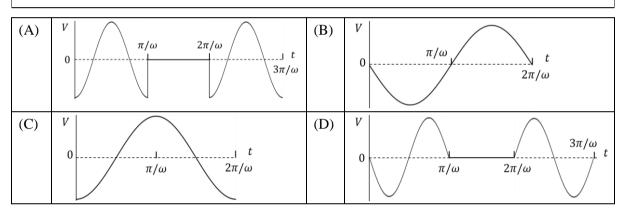
(A)	$\sqrt{\frac{2}{3}\left(\frac{g}{R-r}+\frac{k}{m}\right)}$	(B)	$\sqrt{\frac{2g}{3(R-r)} + \frac{k}{m}}$
(C)	$\sqrt{\frac{1}{6} \left(\frac{g}{R-r} + \frac{k}{m} \right)}$	(D)	$\sqrt{\frac{1}{4} \left(\frac{g}{R-r} + \frac{k}{m} \right)}$

Q.2 In a scattering experiment, a particle of mass 2m collides with another particle of mass m, which is initially at rest. Assuming the collision to be perfectly elastic, the maximum angular deviation θ of the heavier particle, as shown in the figure, in radians is:

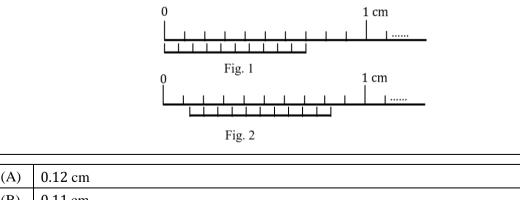


Q.3 A conducting square loop initially lies in the XZ plane with its lower edge hinged along the X-axis. Only in the region $y \ge 0$, there is a time dependent magnetic field pointing along the Z-direction, $\vec{B}(t) = B_0(\cos \omega t)\hat{k}$, where B_0 is a constant. The magnetic field is zero everywhere else. At time t = 0, the loop starts rotating with constant angular speed ω about the X axis in the clockwise direction as viewed from the +X axis (as shown in the figure). Ignoring self-inductance of the loop and gravity, which of the following plots correctly represents the induced e.m.f. (V) in the loop as a function of time:





Q.4 Figure 1 shows the configuration of main scale and Vernier scale before measurement. Fig. 2 shows the configuration corresponding to the measurement of diameter *D* of a tube. The measured value of *D* is:



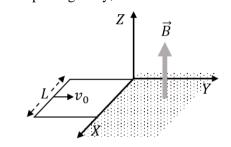
(A)	0.12 cm
(B)	0.11 cm
(C)	0.13 cm
(D)	0.14 cm

SECTION 2 (Maximum Marks: 12)

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

•	Answer to each question will be evaluated according to the following marking scheme :
	Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;
	<i>Partial Marks</i> : +3 If all the four options are correct but ONLY three options are chosen;
	Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;
	Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;
	Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
	Negative Marks : -2 In all other cases.
•	For example, in a question, if (A), (B) and (D) are the ONLY three options corresponding to correct
	answers, then
	choosing ONLY (A), (B) and (D) will get +4 marks;
	choosing ONLY (A) and (B) will get +2 marks;
	choosing ONLY (A) and (D) will get +2 marks;
	choosing ONLY (B) and (D) will get +2 marks;
	choosing ONLY (A) will get +1 mark;
	choosing ONLY (B) will get +1 mark;
	choosing ONLY (D) will get +1 mark;
	choosing no option (i.e. the question is unanswered) will get 0 marks; and
	choosing any other combination of options will get -2 marks.

Q.5 A conducting square loop of side *L*, mass *M* and resistance *R* is moving in the *XY* plane with its edges parallel to the *X* and *Y* axes. The region $y \ge 0$ has a uniform magnetic field, $\vec{B} = B_0 \hat{k}$. The magnetic field is zero everywhere else. At time t = 0, the loop starts to enter the magnetic field with an initial velocity $v_0 \hat{j}$ m/s, as shown in the figure. Considering the quantity $K = \frac{B_0^2 L^2}{RM}$ in appropriate units, ignoring self-inductance of the loop and gravity, which of the following statements is/are correct:



(A)	If $v_0 = 1.5KL$, the loop will stop before it enters completely inside the region of magnetic field.
(B)	When the complete loop is inside the region of magnetic field, the net force acting on the loop is zero.
(C)	If $v_0 = \frac{KL}{10}$, the loop comes to rest at $t = \left(\frac{1}{K}\right) \ln\left(\frac{5}{2}\right)$.
(D)	If $v_0 = 3KL$, the complete loop enters inside the region of magnetic field at time $t = \left(\frac{1}{K}\right) \ln \left(\frac{3}{2}\right)$.

Q.6 Length, breadth and thickness of a strip having a uniform cross section are measured to be 10.5 cm, 0.05 mm, and 6.0 μ m, respectively. Which of the following option(s) give(s) the volume of the strip in cm³ with correct significant figures:

(A) 3.2×10^{-5}	(B)	32.0×10^{-6}	(C)	3.0×10^{-5}	(D)	3×10^{-5}

Q.7 Consider a system of three connected strings, S_1 , S_2 and S_3 with uniform linear mass densities μ kg/m, 4μ kg/m and 16μ kg/m, respectively, as shown in the figure. S_1 and S_2 are connected at the point *P*, whereas S_2 and S_3 are connected at the point *Q*, and the other end of S_3 is connected to a wall. A wave generator 0 is connected to the free end of S_1 . The wave from the generator is represented by $y = y_0 \cos(\omega t - kx)$ cm, where y_0 , ω and *k* are constants of appropriate dimensions. Which of the following statements is/are correct:

(A)	When the wave reflects from <i>P</i> for the first time, the reflected wave is represented by $y = \alpha_1 y_0 \cos(\omega t + kx + \pi)$ cm, where α_1 is a positive constant.
(B)	When the wave transmits through P for the first time, the transmitted wave is represented by $y = \alpha_2 y_0 \cos(\omega t - kx)$ cm, where α_2 is a positive constant.
(C)	When the wave reflects from Q for the first time, the reflected wave is represented by $y = \alpha_3 y_0 \cos(\omega t - kx + \pi)$ cm, where α_3 is a positive constant.
(D)	When the wave transmits through Q for the first time, the transmitted wave is represented by $y = \alpha_4 y_0 \cos(\omega t - 4kx)$ cm, where α_4 is a positive constant.

SECTION 3 (Maximum Marks: 24)

- This section contains SIX (06) questions.
- The answer to each question is a NUMERICAL VALUE.
- For each question, enter the correct numerical value of the answer using the mouse and the onscreen virtual numeric keypad in the place designated to enter the answer.
- If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme:
 Full Marks : +4 If ONLY the correct numerical value is entered in the designated place;
 Zero Marks : 0 In all other cases.
- Q.8 A person sitting inside an elevator performs a weighing experiment with an object of mass 50 kg. Suppose that the variation of the height y (in m) of the elevator, from the ground, with time t (in s) is given by $y = 8 \left[1 + \sin \left(\frac{2\pi t}{T} \right) \right]$, where $T = 40\pi$ s. Taking acceleration due to gravity, g = 10 m/s², the maximum variation of the object's weight (in N) as observed in the experiment is _____

Q.9 A cube of unit volume contains 35×10^7 photons of frequency 10^{15} Hz. If the energy of all the photons is viewed as the average energy being contained in the electromagnetic waves within the same volume, then the amplitude of the magnetic field is $\alpha \times 10^{-9}$ T. Taking permeability of free space $\mu_0 = 4\pi \times 10^{-7}$ Tm/A, Planck's constant $h = 6 \times 10^{-34}$ Js and $\pi = \frac{22}{7}$, the value of α is ______

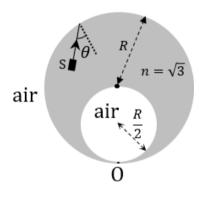
T_Q

Tρ

TP

To

Q.11 A solid glass sphere of refractive index $n = \sqrt{3}$ and radius *R* contains a spherical air cavity of radius $\frac{R}{2}$, as shown in the figure. A very thin glass layer is present at the point O so that the air cavity (refractive index n = 1) remains inside the glass sphere. An unpolarized, unidirectional and monochromatic light source *S* emits a light ray from a point inside the glass sphere towards the periphery of the glass sphere. If the light is reflected from the point O and is fully polarized, then the angle of incidence at the inner surface of the glass sphere is θ . The value of sin θ is _____



- Q.12 A single slit diffraction experiment is performed to determine the slit width using the equation, $\frac{bd}{D} = m\lambda$, where *b* is the slit width, *D* the shortest distance between the slit and the screen, *d* the distance between the m^{th} diffraction maximum and the central maximum, and λ is the wavelength. *D* and *d* are measured with scales of least count of 1 cm and 1 mm, respectively. The values of λ and *m* are known precisely to be 600 nm and 3, respectively. The absolute error (in μ m) in the value of *b* estimated using the diffraction maximum that occurs for m = 3 with d = 5 mm and D = 1 m is ______
- Q.13 Consider an electron in the n = 3 orbit of a hydrogen-like atom with atomic number Z. At absolute temperature T, a neutron having thermal energy $k_{\rm B}T$ has the same de Broglie wavelength as that of this electron. If this temperature is given by $T = \frac{Z^2 h^2}{\alpha \pi^2 a_0^2 m_{\rm N} k_{\rm B}}$, (where h is the Planck's constant, k_B is the Boltzmann constant, $m_{\rm N}$ is the mass of the neutron and a_0 is the first Bohr radius of hydrogen atom) then the value of α is ____

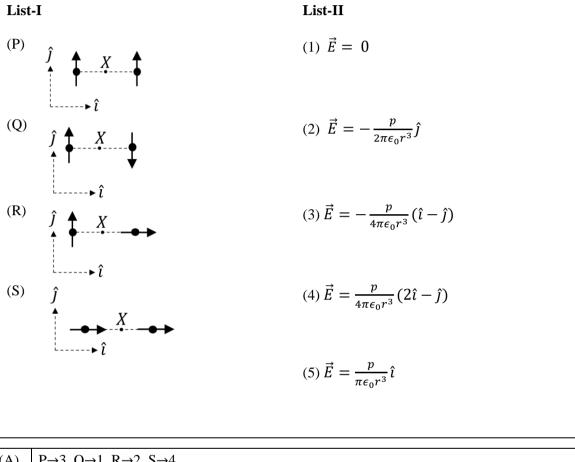
SECTION 4 (Maximum Marks: 12)

- This section contains **THREE (03)** Matching List Sets.
- Each set has **ONE** Multiple Choice Question.
- Each set has TWO lists: List-I and List-II.
- List-I has Four entries (P), (Q), (R) and (S) and List-II has Five entries (1), (2), (3), (4) and (5).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme:
 - *Full Marks* : +4 **ONLY** if the option corresponding to the correct combination is chosen;
 - Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

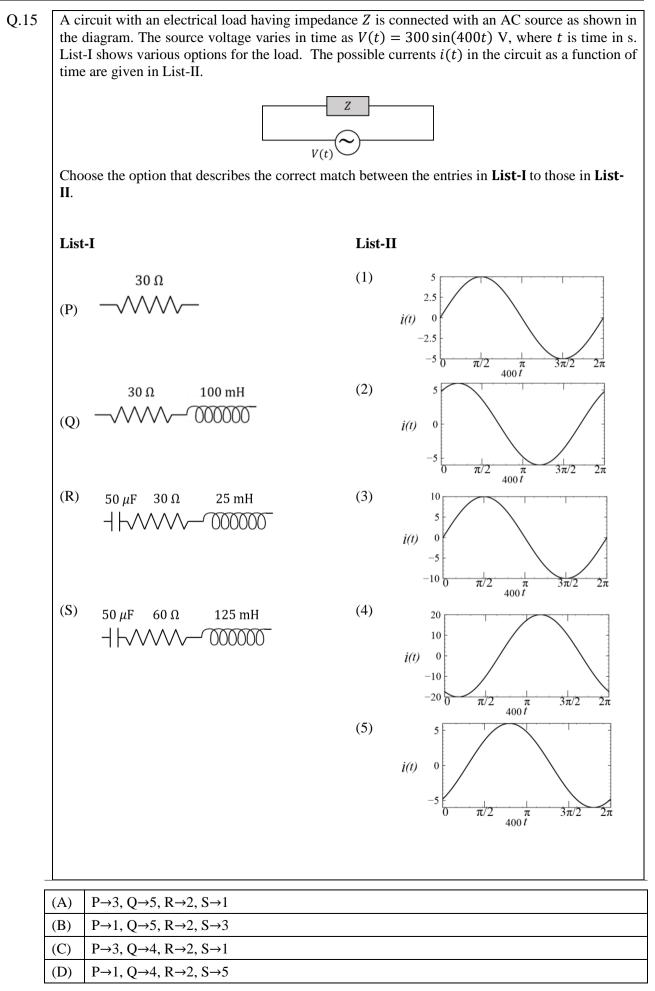
Negative Marks : -1 In all other cases.

Q.14 List-I shows four configurations, each consisting of a pair of ideal electric dipoles. Each dipole has a dipole moment of magnitude p, oriented as marked by arrows in the figures. In all the configurations the dipoles are fixed such that they are at a distance 2r apart along the x direction. The midpoint of the line joining the two dipoles is X. The possible resultant electric fields \vec{E} at X are given in List-II.

Choose the option that describes the correct match between the entries in List-I to those in List-II.



(A)	$P \rightarrow 3, Q \rightarrow 1, R \rightarrow 2, S \rightarrow 4$
(B)	$P \rightarrow 4, Q \rightarrow 5, R \rightarrow 3, S \rightarrow 1$
(C)	$P \rightarrow 2, Q \rightarrow 1, R \rightarrow 4, S \rightarrow 5$
(D)	$P \rightarrow 2, Q \rightarrow 1, R \rightarrow 3, S \rightarrow 5$



(C)

(D)

 $\begin{array}{c|c} P \rightarrow 5, Q \rightarrow 1, R \rightarrow 2, S \rightarrow 4 \\ \hline P \rightarrow 3, Q \rightarrow 2, R \rightarrow 1, S \rightarrow 5 \end{array}$

ass	List-I shows various functional dependencies of energy (<i>E</i>) on the atomic number (<i>Z</i>). Energies associated with certain phenomena are given in List-II.Choose the option that describes the correct match between the entries in List-I to those in List-II.II.						
Lis	:t-I	List-II					
(P)	$E \propto Z^2$	(1) energy of characteristic x-rays					
(Q)	$E \propto (Z-1)^2$	(2) electrostatic part of the nuclear binding energy for stable nuclei with mass numbers in the range 30 to 170					
	$E \propto Z(Z - 1)$ <i>E</i> is practically independent of <i>Z</i>	(3) energy of continuous x-rays(4) average nuclear binding energy per nucleon for stable nuclei with mass number in the range 30 to 170					
		(5) energy of radiation due to electronic transitions from hydrogen-like atoms					
(A)	$P \rightarrow 4, Q \rightarrow 3, R \rightarrow 1, S \rightarrow 2$						
(B)	$P \rightarrow 5, Q \rightarrow 2, R \rightarrow 1, S \rightarrow 4$						

SECTION 1 (Maximum Marks: 12)

- This section contains FOUR (04) questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme: *Full Marks* : +3 If ONLY the correct option is chosen; *Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered); *Negative Marks* : -1 In all other cases.
- Q.1 The heating of NH₄NO₂ at 60–70 °C and NH₄NO₃ at 200–250 °C is associated with the formation of nitrogen containing compounds **X** and **Y**, respectively. **X** and **Y**, respectively, are

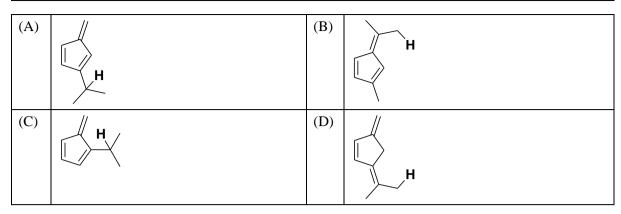
(A)	N ₂ and N ₂ O
(B)	NH ₃ and NO ₂
(C)	NO and N ₂ O
(D)	N ₂ and NH ₃

Q.2 The correct order of the wavelength maxima of the absorption band in the ultraviolet-visible region for the given complexes is

(A)	$[Co(CN)_6]^{3-} < [Co(NH_3)_6]^{3+} < [Co(NH_3)_5(H_2O)]^{3+} < [Co(NH_3)_5(Cl)]^{2+}$
(B)	$[Co(NH_3)_5(Cl)]^{2+} < [Co(NH_3)_5(H_2O)]^{3+} < [Co(NH_3)_6]^{3+} < [Co(CN)_6]^{3-}$
(C)	$[Co(CN)_6]^{3-} < [Co(NH_3)_5(Cl)]^{2+} < [Co(NH_3)_5(H_2O)]^{3+} < [Co(NH_3)_6]^{3+}$
(D)	$[Co(NH_3)_6]^{3_+} < [Co(CN)_6]^{3} < [Co(NH_3)_5(Cl)]^{2_+} < [Co(NH_3)_5(H_2O)]^{3_+}$

Q.3 One of the products formed from the reaction of permanganate ion with iodide ion in neutral aqueous medium is

(A)	I ₂	(B)	IO_3^-	(C)	IO_4^-	(D)	IO_2^-



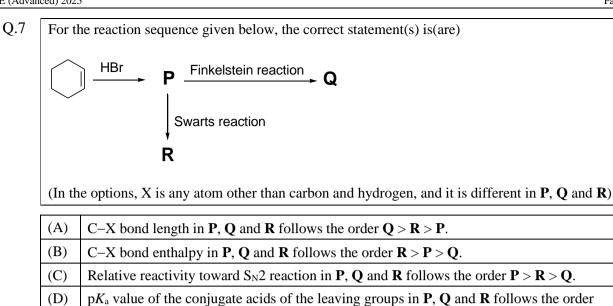
SECTION 2 (Maximum Marks: 12) This section contains THREE (03) questions. Each question has FOUR options (A), (B), (C) and (D). ONE OR MORE THAN ONE of these four option(s) is(are) correct answer(s). For each question, choose the option(s) corresponding to (all) the correct answer(s). Answer to each question will be evaluated according to the following marking scheme: Full Marks : +4 **ONLY** if (all) the correct option(s) is(are) chosen; *Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen; *Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct; *Partial Marks* : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option; 0 If none of the options is chosen (i.e. the question is unanswered); Zero Marks : *Negative Marks* : -2 In all other cases. For example, in a question, if (A), (B) and (D) are the ONLY three options corresponding to correct answers, then choosing ONLY (A), (B) and (D) will get +4 marks; choosing ONLY (A) and (B) will get +2 marks; choosing ONLY (A) and (D) will get +2 marks; choosing ONLY (B) and (D) will get +2 marks; choosing ONLY (A) will get +1 mark; choosing ONLY (B) will get +1 mark; choosing ONLY (D) will get +1 mark; choosing no option (i.e. the question is unanswered) will get 0 marks; and choosing any other combination of options will get -2 marks.

Q.5 Regarding the molecular orbital (MO) energy levels for homonuclear diatomic molecules, the **INCORRECT** statement(s) is(are)

(A)	Bond order of Ne ₂ is zero.	
(B)	The highest occupied molecular orbital (HOMO) of F_2 is σ -type.	
(C)	Bond energy of O_2^+ is smaller than the bond energy of O_2 .	
(D)	Bond length of Li_2 is larger than the bond length of B_2 .	

Q.6 The pair(s) of diamagnetic ions is(are)

(A)	La^{3+}, Ce^{4+}
(B)	Yb^{2+}, Lu^{3+}
(C)	La^{2+}, Ce^{3+}
(D)	Yb^{3+}, Lu^{2+}



 $\mathbf{R} > \mathbf{Q} > \mathbf{P}$.

SECTION 3 (Maximum Marks: 24)

- This section contains SIX (06) questions.
- The answer to each question is a **NUMERICAL VALUE.**
- For each question, enter the correct numerical value of the answer using the mouse and the onscreen virtual numeric keypad in the place designated to enter the answer.
- If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme:

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Full Marks: +4If ONLY the correct numerical value is entered in the designated place;Zero Marks: 0In all other cases.
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Q.8 In an electrochemical cell, dichromate ions in aqueous acidic medium are reduced to Cr^{3+} . The current (in amperes) that flows through the cell for 48.25 minutes to produce 1 mole of Cr^{3+} is _____.

Use: 1 Faraday = 96500 C mol^{-1}

Q.9 At 25 °C, the concentration of H⁺ ions in 1.00×10^{-3} M aqueous solution of a weak monobasic acid having acid dissociation constant (K_a) of 4.00×10^{-11} is $X \times 10^{-7}$ M. The value of X is _____.

Use: Ionic product of water $(K_w) = 1.00 \times 10^{-14}$ at 25 °C

Q.10 Molar volume ($V_{\rm m}$) of a van der Waals gas can be calculated by expressing the van der Waals equation as a cubic equation with $V_{\rm m}$ as the variable. The ratio (in mol dm⁻³) of the coefficient of $V_{\rm m}^2$ to the coefficient of $V_{\rm m}$ for a gas having van der Waals constants a = 6.0 dm⁶ atm mol⁻² and b = 0.060dm³ mol⁻¹ at 300 K and 300 atm is _____.

Use: Universal gas constant (R) = $0.082 \text{ dm}^3 \text{ atm mol}^{-1} \text{ K}^{-1}$

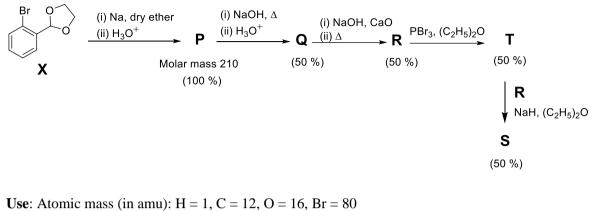
Q.11 Considering ideal gas behavior, the expansion work done (in kJ) when 144 g of water is electrolyzed completely under constant pressure at 300 K is _____.

Use: Universal gas constant (R) = 8.3 J K⁻¹ mol⁻¹; Atomic mass (in amu): H = 1, O = 16

Q.12 The monomer (**X**) involved in the synthesis of Nylon 6,6 gives positive carbylamine test. If 10 moles of **X** are analyzed using Dumas method, the amount (in grams) of nitrogen gas evolved is

Use: Atomic mass of N (in amu) = 14

Q.13 The reaction sequence given below is carried out with 16 moles of **X**. The yield of the major product in each step is given below the product in parentheses. The amount (in grams) of **S** produced is_____.



SECTION 4 (Maximum Marks: 12)

- This section contains **THREE (03)** Matching List Sets.
- Each set has **ONE** Multiple Choice Question.
- Each set has TWO lists: List-I and List-II.
- List-I has Four entries (P), (Q), (R) and (S) and List-II has Five entries (1), (2), (3), (4) and (5).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme:
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 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
 Negative Marks : -1 In all other cases.

Q.14 The correct match of the group reagents in **List-I** for precipitating the metal ion given in **List-II** from solutions, is

List-I	List-II
 (P) Passing H₂S in the presence of NH₄OH (Q) (NH₄)₂CO₃ in the presence of NH₄OH (R) NH₄OH in the presence of NH₄Cl (S) Passing H₂S in the presence of dilute HCl 	(1) Cu ²⁺ (2) Al ³⁺ (3) Mn ²⁺ (4) Ba ²⁺ (5) Mg ²⁺

(A)	$P \rightarrow 3; Q \rightarrow 4; R \rightarrow 2; S \rightarrow 1$
(B)	$P \rightarrow 4; Q \rightarrow 2; R \rightarrow 3; S \rightarrow 1$
(C)	$P \rightarrow 3; Q \rightarrow 4; R \rightarrow 1; S \rightarrow 5$
(D)	$P \rightarrow 5; Q \rightarrow 3; R \rightarrow 2; S \rightarrow 4$

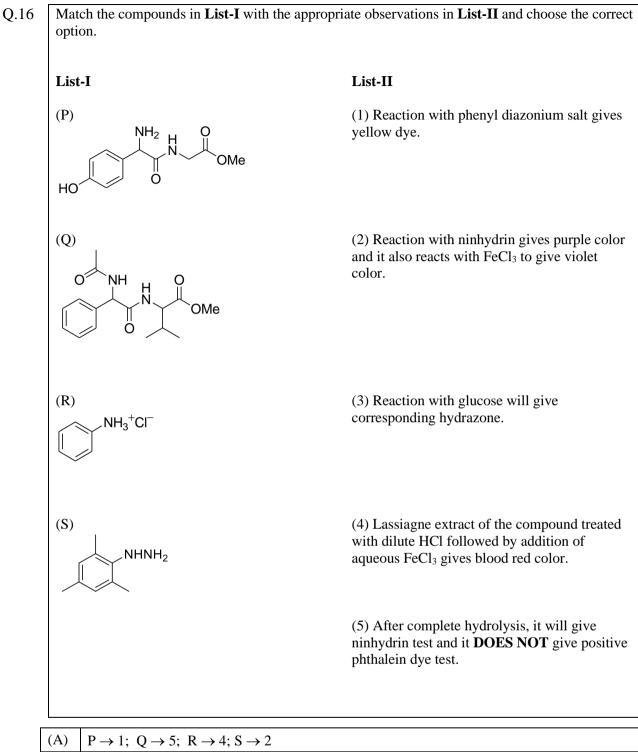
 Q.15
 The major products obtained from the reactions in List-II are the reactants for the named reactions mentioned in List-I. Match each entry in List-I with the appropriate entry in List-II and choose the correct option.

 List-I
 List-II

 (P) Stephen reaction
 (1)

	Toluene $\frac{(i) CrO_2 CI_2 / CS_2}{(ii) H_3 O^+}$
(Q) Sandmeyer reaction	(2) (i) PCI ₅ (ii) NH ₃
	Benzoic acid $(iii) P_4 O_{10}, \Delta$
(R) Hoffmann bromamide degradation reaction	(3) (i) Fe, HCl (ii) HCl, NaNO ₂ (273-278 K), H ₂ O
	Nitrobenzene
(S) Cannizzaro reaction	(4) (i) Cl ₂ /hv, H ₂ O
	(ii) Tollen's reagent (iii) SO ₂ Cl ₂ Toluene (iv) NH ₃
	(5) (i) (CH ₃ CO) ₂ O, Pyridine (ii) HNO ₃ , H ₂ SO ₄ , 288 K
	Aniline (iii) aq. NaOH
(A) $P \rightarrow 2; Q \rightarrow 4; R \rightarrow 1; S \rightarrow 3$	
(B) $P \rightarrow 2: O \rightarrow 3: R \rightarrow 4: S \rightarrow 1$	

(\mathbf{A})	$P \rightarrow 2; Q \rightarrow 4; R \rightarrow 1; S \rightarrow S$
(B)	$P \rightarrow 2; Q \rightarrow 3; R \rightarrow 4; S \rightarrow 1$
(C)	$P \rightarrow 5; Q \rightarrow 3; R \rightarrow 4; S \rightarrow 2$
(D)	$P \rightarrow 5; Q \rightarrow 4; R \rightarrow 2; S \rightarrow 1$



()	
(B)	$P \rightarrow 2; Q \rightarrow 5; R \rightarrow 1; S \rightarrow 3$
(C)	$P \rightarrow 5; Q \rightarrow 2; R \rightarrow 1; S \rightarrow 4$
(D)	$P \rightarrow 2; Q \rightarrow 1; R \rightarrow 5; S \rightarrow 3$

END OF THE QUESTION PAPER